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Alexandria Engineering Journal

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ORIGINAL ARTICLE

Second law analysis for hydromagnetic couple stress fluid flow through a porous channel



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Received 14 October 2015; revised 20 February 2016; accepted 21 February 2016

Available online 5 March 2016

KEYWORDS

Magnetic field;
 Entropy generation;
 Slip flow;
 Irreversibility ratio;
 ADM;
 Ohmic heating

Abstract In this work, the combined effects of magnetic field and ohmic heating on the entropy generation rate in the flow of couple stress fluid through a porous channel are investigated. The equations governing the fluid flow are formulated, non-dimensionalised and solved using a rapidly convergent semi-analytical Adomian decomposition method (ADM). The result of the computation shows a significant dependence of fluid's thermophysical parameters on Joule's dissipation as well as decline in the rate of change of fluid momentum due to the interplay between Lorentz and viscous forces. Moreover, the rate of entropy generation in the flow system drops as the magnitude of the magnetic field increases.

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1. Introduction

In recent times, there has been a renewed interest in the thermodynamic analysis involving channel fluid flows. This is due to the usefulness of the study in several renewable energy applications. For instance, it could be used to predict the efficiency of many thermal systems exchanging heat between two heat reservoirs and other Carnot systems. Moreover, in the energy generation, excessive energy is wasted or dissipated in the form of heat. Hence there is need to minimise the wastage by improving the energy of the system. Based on this fact, few

research works have been reported in the literature. For example, Adesanya and Makinde [1] reported the entropy generation in couple stress fluid flowing steadily through a porous channel with slip at the isothermal walls. Similarly, Adesanya and Makinde [2] studied the entropy generation rate in the couple stress fluid flowing through a porous channel with convective heating at the walls. Also in the class of couple stress fluid, Makinde and Eegunjobi [3] investigated the inherent irreversibility of heat in steady flow of a couple stress fluid through a vertical channel filled with porous materials. Other important work on the entropy generation in a moving fluid includes [4–7].

In all the studies above on the thermodynamics analysis, the effect of magnetic field, placed in the transverse direction to the flow channel has been neglected. In reality, magnetic field plays a vital role in many industrial and thermal engineering applications. For instance, it is useful in controlling extremely hot moving fluid like molten steel and many more.

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Peer review under responsibility of Faculty of Engineering, Alexandria University.

<http://dx.doi.org/10.1016/j.aej.2016.02.020>

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Nomenclature

β_1	dimensionless Navier slip parameter at the lower wall	E_G	volumetric rate of entropy
β_2	dimensionless Navier slip parameter at the upper wall	G	dimensionless pressure gradient
η	coefficient of couple stress	h	width of the channel
γ_1	Navier slip coefficient at the lower plate	H^2	Hartmann number
γ_2	Navier slip coefficient at the upper plate	N_1	entropy generation due to heat transfer
κ	thermal conductivity	N_2	entropy generation due to entropy generation due to fluid friction and ohmic heating
μ	dynamic viscosity	N_s	entropy generation number
Ω	parameter that measures the temperature difference between the two heat reservoirs	Pr	Prandtl number
ρ	fluid density	s	suction/injection parameter
σ_e	electrical conductivity	T	fluid temperature
θ	dimensionless fluid temperature	T_0	temperature at the lower plate
a^2	couple stress parameter	T_f	final fluid temperature
B_0	magnetic field strength	u	dimensionless fluid velocity
Br	Brinkman number	u'	fluid velocity
c_p	specific heat at constant pressure	v_0	uniform suction/injection velocity
		x', y'	cartesian coordinates
		x, y	dimensionless cartesian coordinates

Several researchers have investigated the entropy analysis in hydromagnetic fluid flow in recent times. For example, Das and Jana [8] presented the second law analysis for magnetohydrodynamic incompressible fluid flow through a porous channel by imposing Navier slip conditions at the walls. Adesanya and Falade [9] analysed the inherent irreversibility in the flow of hydrodynamic third grade fluid through a channel saturated with porous materials. Similarly, the effect of hall current was presented in a study by Das and Jana [10]. Interested readers can see more interesting work on the influence of magnetic field on entropy generation rate in Refs. [11–20].

Motivated by studies in [8–20], the objective of the present study was to examine the influence of magnetic field and ohmic heating of the couple stress fluid on the entropy production within the flow channel, which has not been accounted for in the literature. The outcoming results are expected to enhance many industrial and thermal engineering processes whose working medium is a non-Newtonian fluid, with a view to minimise entropy generation which tends to deplete the amount of available energy for work.

To achieve this objective, flow governing equations are formulated, and non-dimensionalised and approximate solution of the dimensionless coupled non-linear boundary-value problem are obtained by using a semi-analytical Adomian decomposition method [21,22]. The choice of the method is due to the fact that the method does not require any linearisation, discretisation, use of initial guess or perturbation. These approximation solutions are used to compute the entropy generation rate and irreversibility ratio.

In the following section, the problem is formulated and non-dimensional analysis is also presented. Section 3 of the work contains the method of solution, results are presented and discussed in Section 4, while Section 5 concludes the paper.

2. Mathematical formulation

A fully developed hydromagnetic non-Newtonian fluid flow between two parallel plates is considered. The parallel plates

are infinite, permeable and stationary relative to the fluid motion as shown in Fig. 1. We choose a 2-dimensional cartesian coordinate system with x -axis along the flow direction and y -axis orthogonal to the planes of the parallel plates, separated by width $y = h$. Fluid injection occurs at the lower plate at a uniform rate v_0 , matched with a corresponding fluid suction at the upper plate. A constant magnetic field of strength B_0 is applied perpendicular to the direction of fluid flow. For most industrial applications, a non-chaotic fluid flow is desired such that the magnetic Reynolds number is very small, and since no external voltage is applied to the fully developed flow system, the induced magnetic field and Hall effect are negligible. We further assumed that all the fluid properties are constant and the Stokes constitutive model for the couple stresses is used. Consequently, the momentum and energy balance equations, with the local volumetric entropy generation rate (E_G) for the fluid flow can be written as follows [1,10]:

$$v_0 \rho \frac{du'}{dy'} = -\frac{dP}{dx'} + \mu \frac{d^2 u'}{dy'^2} - \eta \frac{d^4 u'}{dy'^4} - \sigma_e B_0^2 u', \quad (1)$$

$$\rho c_p v_0 \frac{dT}{dy'} = \kappa \frac{d^2 T}{dy'^2} + \mu \left(\frac{du'}{dy'} \right)^2 + \eta \left(\frac{d^2 u'}{dy'^2} \right)^2 + \sigma_e B_0^2 u'^2, \quad (2)$$

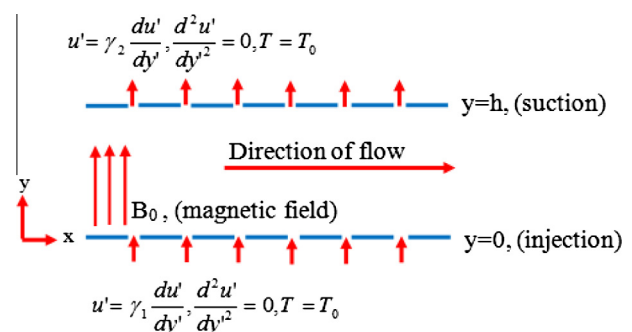


Figure 1 The geometry of the model.

$$E_G = \frac{\kappa}{T_0^2} \left(\frac{dT}{dy'} \right)^2 + \frac{\mu}{T_0} \left(\frac{du'}{dy'} \right)^2 + \frac{\eta}{T_0} \left(\frac{d^2u'}{dy'^2} \right)^2 + \frac{\sigma_e}{T_0} B_0^2 u^2, \quad (3)$$

with the boundary conditions

$$u'(0) = \gamma_1 \frac{du'(0)}{dy'}, \quad \frac{d^2u'(0)}{dy'^2} = 0, \quad T(0) = T_0, \quad (4)$$

$$u'(1) = \gamma_2 \frac{du'(1)}{dy'}, \quad \frac{d^2u'(1)}{dy'^2} = 0, \quad T(1) = T_0, \quad (5)$$

where u' and P are the fluid velocity and pressure respectively, v_0 is the injection/suction velocity at the channel walls, η is the coefficient of couple stress, μ is the dynamic viscosity, γ_i corresponds to the Navier slip coefficients at the lower plate and upper plate, respectively for $i = 1, 2$, ρ is the fluid density, σ_e is the fluid electrical conductivity, κ is the coefficient of thermal conductivity, c_p is the isobaric specific heat, T_f and T_0 are referenced fluid temperatures, and T is the fluid temperature. The present model has potential application in automated heat control mechanisms, especially in micro-channels. It is often desired in manufacturing processes that the rate of randomness (or entropy generation) be tamed to avoid system complexity.

Introducing the following dimensionless parameters and variables,

$$y = \frac{y'}{h}, \quad u = \frac{u'}{v_0}, \quad \theta = \frac{T - T_0}{T_f - T_0}, \quad s = \frac{v_0 h}{\nu}, \quad G = -\frac{h^2}{\mu v_0} \frac{dP}{dx'},$$

$$a^2 = \frac{\mu h^2}{\eta}, \quad H^2 = \frac{\sigma_e h^2 B_0^2}{\mu}, \quad Pr = \frac{v_0 c_p}{\kappa}, \quad Br = \frac{v_0^2 \mu}{\kappa(T_f - T_0)}, \quad (6)$$

$$\Omega = \frac{T_f - T_0}{T_0}, \quad N_s = \frac{T_0^2 h^2 E_G}{\kappa(T_f - T_0)^2}, \quad \beta_1 = \frac{\gamma_1}{h}, \quad \beta_2 = \frac{\gamma_2}{h},$$

we obtain the following boundary value problems:

$$s \frac{du}{dy} = G + \frac{d^2u}{dy^2} - \frac{1}{a^2} \frac{d^4u}{dy^4} - H^2 u, \quad (7)$$

$$sPr \frac{d\theta}{dy} = \frac{d^2\theta}{dy^2} + Br \left(\frac{du}{dy} \right)^2 + \frac{Br}{a^2} \left(\frac{d^2u}{dy^2} \right)^2 + BrH^2 u^2, \quad (8)$$

together with the boundary conditions

$$u(0) = \beta_1 \frac{du(0)}{dy}, \quad \frac{d^2u(0)}{dy^2} = 0, \quad \theta(0) = 0$$

$$u(1) = \beta_2 \frac{du(1)}{dy}, \quad \frac{d^2u(1)}{dy^2} = 0, \quad \theta(1) = 0, \quad (9)$$

while the entropy generation can be computed using

$$N_s = \left(\frac{d\theta}{dy} \right)^2 + \frac{Br}{\Omega} \left(\frac{du}{dy} \right)^2 + \frac{Br}{\Omega a^2} \left(\frac{d^2u}{dy^2} \right)^2 + \frac{Br}{\Omega} H^2 u^2. \quad (10)$$

Our model given by Eqs. (7), (8) and (10) reduces to the asymptotic case as $H^2 \rightarrow 0$ as obtained in Ref. [1].

3. Adomian decomposition method of solution

In this section, we seek the solution of the model Eqs. (7), (8) and (10) subject to the boundary condition (9), using the semi-analytical Adomian decomposition scheme. To achieve this, the boundary value problems are converted to the equivalent integral equations noting that $u''(0) = u''(1) = 0$. Thus,

$$u(y) = f_0 + f_1 y + \frac{y^3}{6} f_2 + a^2 \int_0^y \int_0^y \int_0^y \int_0^y F_4(Y) dY dY dY dY, \quad (11)$$

$$\theta(y) = c_0 + c_1 y + \int_0^y \int_0^y (F_2(Y) - BrH^2 u^2) dY dY \quad (12)$$

where

$$F_4(Y) = G + \frac{d^2u}{dY^2} - s \frac{du}{dY} - H^2 u,$$

$$F_2(Y) = sPr \frac{d\theta}{dY} - Br \left(\frac{du}{dY} \right)^2 - \frac{Br}{a^2} \left(\frac{d^2u}{dY^2} \right)^2.$$

The unknown coefficients f_0, f_1, f_2, c_0 and c_1 are to be determined by using the method of undetermined coefficients. Following ADM we seek solutions in the form of an infinite series:

$$u(y) = \sum_0^\infty u_n(y), \quad \theta(y) = \sum_0^\infty \theta_n(y). \quad (13)$$

Substituting (13) into (11) and (12), we obtain

$$\sum_{n=0}^\infty u_n(y) = f_0 + f_1 y + \frac{y^3}{6} f_2 + a^2 L_4(Y) dY dY dY dY, \quad (14)$$

and

$$\sum_{n=0}^\infty \theta_n(y) = c_0 + c_1 y + \int_0^y \int_0^y (Z_1 - Z_2) dY dY; \quad (15)$$

where

$$L_4(Y) = \int_0^y \int_0^y \int_0^y \int_0^y \left(G + \sum_{n=0}^\infty \frac{d^2u_n}{dY^2} - s \sum_{n=0}^\infty \frac{du_n}{dY} - H^2 \sum_{n=0}^\infty u_n \right),$$

$$Z_1 = sPr \sum_{n=0}^\infty \frac{d\theta_n}{dY} - Br \sum_{n=0}^\infty \left(\frac{du_n}{dY} \right)^2,$$

and

$$Z_2 = \frac{Br}{a^2} \sum_{n=0}^\infty \left(\frac{d^2u_n}{dY^2} \right)^2 - BrH^2 \sum_{n=0}^\infty u_n^2.$$

Evidently (13) may be written in the recursive form:

$$u_0(y) = f_0 + f_1 y + \frac{y^3}{6} f_2 + a^2 \int_0^y \int_0^y \int_0^y \int_0^y G dY dY dY dY, \quad (16)$$

$$u_{n+1}(y) = a^2 \int_0^y \int_0^y \left(\frac{d^2u_n}{dY^2} - s \frac{du_n}{dY} - H^2 u_n \right) dY dY. \quad (17)$$

In order to reduce the computational load in (15), the modified recurrent relation

$$\theta_0(y) = c_1 y, \quad (18)$$

is used, so that

$$\theta_1(y) = \int_0^y \int_0^y \left(sPr \sum_{n=0}^\infty \frac{d\theta_0}{dY} - \frac{Br}{a^2} \left(\frac{d^2u}{dY^2} \right)^2 \right) dY dY. \quad (19)$$

$$\theta_2(y) = \int_0^y \int_0^y \left(sPr \sum_{n=0}^\infty \frac{d\theta_1}{dY} - Br \left(\frac{du}{dY} \right)^2 \right) dY dY. \quad (20)$$

$$\theta_3(y) = \int_0^y \int_0^y \left(sPr \sum_{n=0}^{n=\infty} \left(\frac{d\theta_2}{dY} - BrH^2u^2 \right) dY dY \right) \quad (21)$$

$$\theta_{n+1}(y) = \int_0^y \int_0^y \left(sPr \sum_{n=0}^{n=\infty} \frac{d\theta_n}{dY} \right) dY dY; \quad (n \geq 2), \quad (22)$$

Due to convergence of the ADM series solution conducted in Ref. [6] only few terms of the series will be required to obtain the approximate solutions of the problem. We set the number of iteration to m so that the approximate solutions (13) may be written as the finite series as follows:

$$u(y) = \sum_0^m u_n(y), \quad \theta(y) = \sum_0^m \theta_n(y). \quad (23)$$

The irreversibility in the heat flow to the viscous fluid is analysed using (10) by expressing the entropy generation number N_s as partial sum of the entropy generation due to heat transfer, and the irreversibility resulting from fluid friction and ohmic heating of the fluid. Therefore we set N_1 and N_2 as follows:

$$N_1 = \left(\frac{d\theta}{dy} \right)^2, \quad N_2 = \frac{Br}{\Omega} \left(\frac{du}{dy} \right)^2 + \frac{Br}{\Omega a^2} \left(\frac{d^2u}{dy^2} \right)^2 + \frac{Br}{\Omega} H^2 u^2. \quad (24)$$

The Bejan number Be , which is a parameter that measures the irreversibility ratio in the heat flow, may be defined as

$$Be = \frac{N_1}{N_s} = \frac{1}{1 + \Phi}, \quad \Phi = \frac{N_2}{N_1}. \quad (25)$$

where Φ is the irreversibility ratio, a parameter that measures the rate of destruction of available work in the flow system. The Bejan number in Eq. (25) is bounded in the interval $0 \leq Be \leq 1$. The irreversibility due to heat transfer is dominant when $Be = 1$, while the irreversibility due to viscosity and magnetic field is dominant when $Be = 0$. The dimensionless Eqs. (7)–(10), with the boundary conditions (9) were solved using the algorithm in (16)–(23), coded in MATHEMATICA symbolic package. Using the numerical procedure discussed above, we computed the dimensionless velocity, temperature, entropy generation and irreversibility ratio. In what follows, we discussed some interesting results from our findings.

4. Results and discussion

Let us begin by examining the effect of the applied magnetic field and couple stresses on the flow velocity, the variations of the dimensionless velocity with the width of the flow channel as presented in Fig. 2, for varying values of magnetic parameter (Hatman number, H^2), couple stress inverse parameter a^2 , suction/injection parameter s , upper wall Navier-slip parameter β_2 , and lower wall Navier-slip parameter β_1 . We showed in Table 1 that the ADM could guarantee a result comparable with the exact solution of the problem, with absolute error of order 10^{-7} for $m = 4$. It is clear from Fig. 2a that by increasing the magnetic field the flow velocity would be inhibited. This could be explained by the action of Lorentz force, whose presence in the flow system constitutes resistance to the momentum of fluid parcels in the adjacent fluid layers.

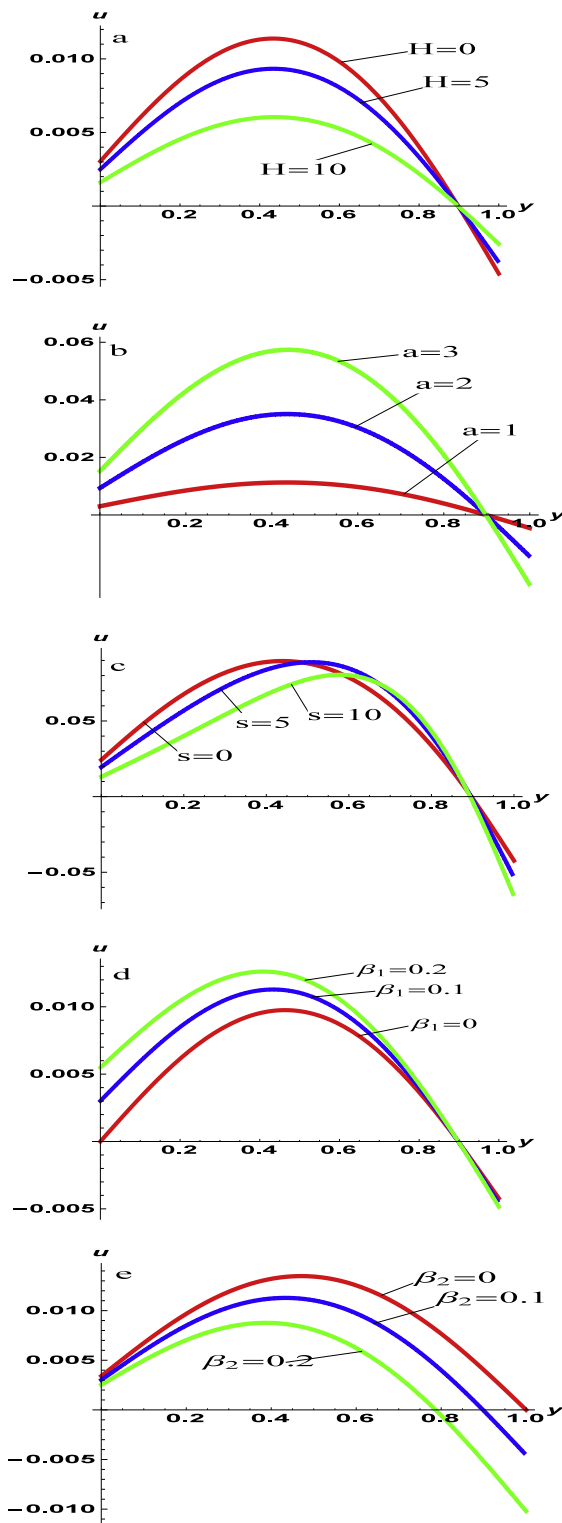


Figure 2 Parameterised velocity profiles of the fluid flow: (a) at varying Hatman number H , with $a = s = 1, \beta_1 = \beta_2 = 0.1$; (b) at varying couple stress inverse a , with $H = s = 1, \beta_1 = \beta_2 = 0.1$; (c) at varying suction/injection parameter s , with $H = 1, a = 5, \beta_1 = \beta_2 = 0.1$; (d) at varying lower wall Navier-slip parameter β_1 , with $H = a = s = 1, \beta_2 = 0.1$; (e) at varying upper wall Navier-slip parameter β_2 , with $H = a = s = 1, \beta_1 = 0.1$.

Fig. 2b depicts the implication of increasing couple stress inverse parameter on the flow velocity. Here, we find that an increase in couple stress inverse parameter corresponds to increase in fluid friction in the moving fluid. This friction arises from the effect of particle additives, constituting size dependent effect on couple stress fluids. Moreover, rotational field of the velocity is generated in couple stress fluid. Hence, an increase in couple stress results in decrease in the velocity profile of the fluid. Fig. 2c shows the effect of suction/injection on the velocity profile of the fluid flow. Clearly, the increase in suction/injection parameter breaks the symmetry of the fluid flow. This is because the continual injection of fluid into the channel, from a direction different from that of channel fluid flow, changes the momentum of (or slows down) the fluid parcels at the lower wall-fluid interface. This effect is propagated beyond the neighbourhood of the lower plate, which breaks the symmetry of the channel flow system. However, increasing the suction/injection parameter does not show any significant effect at the upper wall of the channel. Fig. 2d and e depicts the effects of Navier-slip parameters on the velocity profile of the fluid flow. Evidently, the fluid slippage has significant effect on the fluid motion, in that any change in any of the parameters impacts on the viscous drag on the flow, which scales the maximum velocity of the flow up or down. In clear terms, increasing the upper wall Navier-slip parameter decreases the fluid velocity significantly at the upper wall as well as the maximum velocity of the fluid flow. In contrast, increasing the slip parameter at the lower wall increases the velocity at the wall as well as the maximum velocity of the fluid flow.

Next we describe the temperature response of the fluid with respect to flow to changes in the values of the magnetic parameter, couple stress parameter and the Brinkman number Fig. 3. Fig. 3a shows that increasing the magnetic field intensity (or parameter) translates into a decrease in the channel temperature. Fig. 3b reveals that increasing couple stresses decrease the temperature profile in the channel. Expectedly, couple stresses enhance the fluid's intermolecular cohesion. This increases the fluid's resistance to shear stress, resulting in temperature rise within the flow channel. Fig. 3c shows that an increase in Brinkman number results in the increase in the fluid temperature.

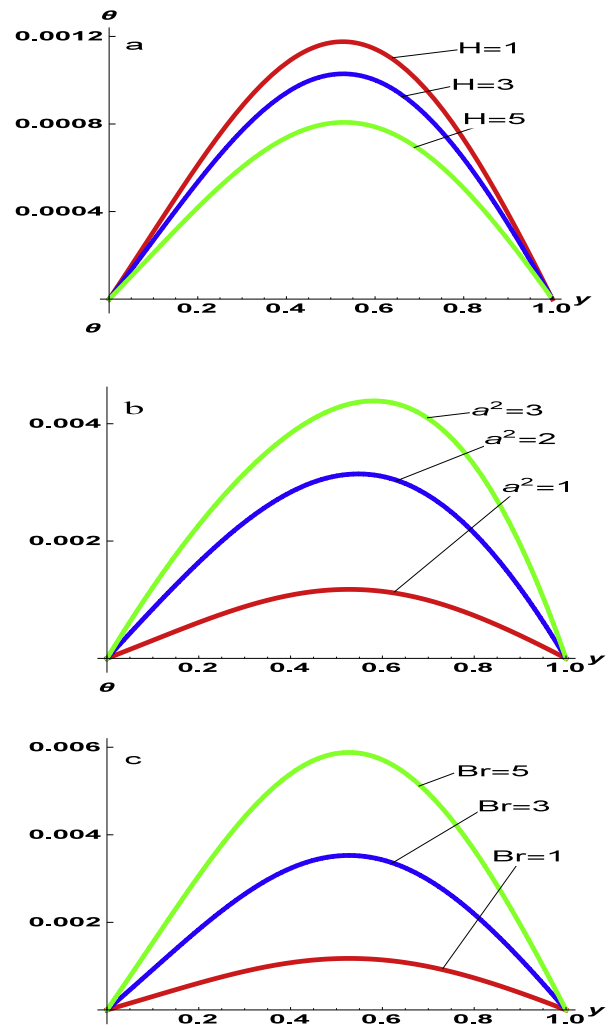


Figure 3 Parameterised temperature profiles of the fluid flow: (a) at varying values of Hatman number H , with $a = s = Br = 1$, $Pr = 0.71$, $\beta_1 = \beta_2 = 0.1$; (b) at varying values of couple stress inverse a , with $H = s = Br = 1$, $Pr = 0.71$, $\beta_1 = \beta_2 = 0.1$; (c) at varying values of the Brinkman number Br , with $H = a = s = 1$, $Pr = 0.71$, $\beta_1 = \beta_2 = 0.1$.

Table 1 Comparison between analytical and exact solution for the velocity profile for the parameters $a = 1$, $H = 0.2$, $s = \beta_1 = \beta_2 = 0.1$.

u	u_{Exact}	u_{ADM}	Absolute error
0	0.00303054	0.00303070	1.56912×10^{-7}
0.1	0.00598827	0.00598858	3.11550×10^{-7}
0.2	0.00854151	0.00854196	4.52517×10^{-7}
0.3	0.01037320	0.01037370	5.66015×10^{-7}
0.4	0.01125880	0.01125950	6.38135×10^{-7}
0.5	0.01106440	0.01106510	6.55205×10^{-7}
0.6	0.00974517	0.00974577	6.04755×10^{-7}
0.7	0.00734506	0.00734554	4.77423×10^{-7}
0.8	0.00399756	0.00399783	2.70091×10^{-7}
0.9	-0.00007304	-0.00007305	9.47647×10^{-9}
1.0	-0.00454921	-0.00454955	3.36326×10^{-7}

To complete the analysis, the effects of the magnetic parameter, H^2 , couple stress parameter, a^2 , and the Brinkman number, Br on the entropy generation are shown in Fig. 4. Interestingly, it is observed from Fig. 4a that the entropy generation, N_s decreases with increase in magnetic parameter H^2 in the middle of the channel. The interplay between the two thermophysical phenomena, namely the intermolecular cohesion and entropy generation rate in viscous fluid becomes imperative. Viscosity increases as the intermolecular cohesion within the fluid rises, or vice versa. The applied Lorentz force reduces the intermolecular cohesion within the fluid resulting in decrease in entropy generation N_s within the channel flow. Fig. 4b and c shows that the rate of entropy generation increases with increase in both couple stress parameter and the Brinkman number. Increase in Brinkman number raises both dissipations due to Joule heating and viscosity, which in turn increases the entropy generation rate. Fig. 5 shows

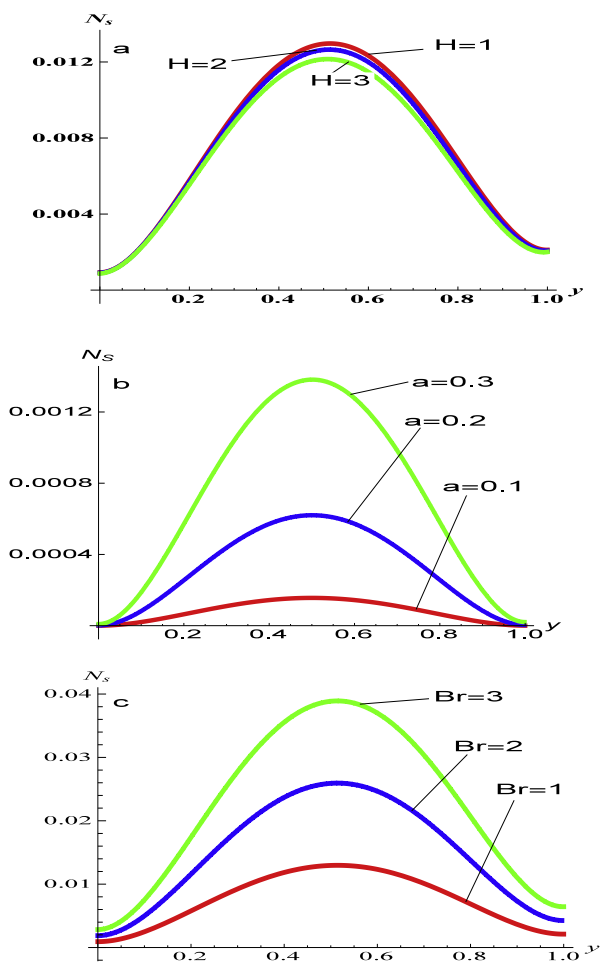


Figure 4 Entropy generation rate: (a) at varying values of Hatman number H , with $a = s = Br = \Omega = 1$, $Pr = 0.71$, $\beta_1 = \beta_2 = 0.1$; (b) at varying values of couple stress inverse a , with $H = s = Br = \Omega = 1$, $Pr = 0.71$, $\beta_1 = \beta_2 = 0.1$; (c) at varying values of the Brinkman number Br , with $H = a = s = \Omega = 1$, $Pr = 0.71$, $\beta_1 = \beta_2 = 0.1$.

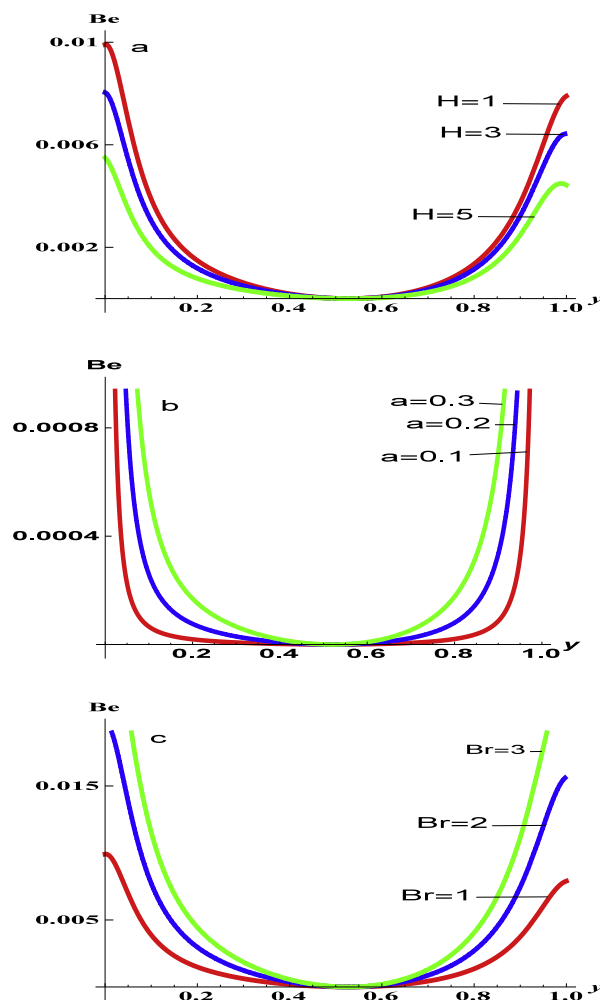


Figure 5 Irreversibility ratio: (a) at varying values of Hatman number H , with $a = s = Br = \Omega = 1$, $Pr = 0.71$, $\beta_1 = \beta_2 = 0.1$; (b) at varying values of couple stress inverse a , with $H = s = Br = \Omega = 1$, $Pr = 0.71$, $\beta_1 = \beta_2 = 0.1$; (c) at varying values of the Brinkman number Br , with $H = a = s = \Omega = 1$, $Pr = 0.71$, $\beta_1 = \beta_2 = 0.1$.

the dominance of fluid viscosity on the irreversibility ratio, over heat transfer at the centreline of the channel. In Fig. 5a, it is observed that as the magnetic parameter H^2 increases, heat transfer dominates the irreversibility ratio at the walls, while Fig. 5a and b revealed that as the couple stress inverse and the Brinkman number increase, fluid viscosity dominates the irreversibility ratio.

Following from the discussion above, at specific $a^2, s, \beta_{1,2}$ and Br , varying the magnetic field automatically changes the fluid's rate of change of momentum, which in turn changes the fluid velocity. Reducing velocity in micro-channel fluid flow effectively reduces fluid temperature, rate of entropy production in the fluid, and the irreversibility ratio as shown in Figs. 2–5.

5. Conclusion

The effects of magnetic field and couple stresses on entropy generation in an MHD flow through a porous channel, with suction/injection and Navier slip have been examined. The Adomian decomposition method was employed to obtain

semi-analytical solution that approximates the velocity and temperature profiles, which are used to obtain the entropy generation production as well as the Bejan number. It was found that the entropy generation rate reduces with increasing magnetic parameter. The magnetic field acts in such a way as to tame the degree of randomness in the fluid's particles, resulting in the lowering of the fluid's velocity and entropy generation rate in the system. In effect, the fluid velocity, the fluid temperature and entropy generation showed significant dependence on Joule dissipation. This result suggests a balanced mix between heat transfer irreversibility and fluid friction irreversibility, which would enhance entropy minimisation and hence system design and manufacturing applications. Our result would motivate applications in micro-channel automatic heat control systems.

Acknowledgement

UEV is supported by the Royal Society of London, through their Newton International Fellowship Alumni scheme.

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